

Year 6

Key Mathematical Concepts and representations

Number and Place Value

Year 6

Powers of 10 (1)

Vocabulary:

Tens Hundreds Thousands Ten-thousands Hundred-thousands Ones Digit Place Value Millions Ten-Millions Tenths Hundredths Represents Gattegno Tens Frame Equivalent Equation Multiply Divide Counters

One-tenth/hundredth times the size Ten/hundred times the size

M	lillions	3	Thousands				Ones		-t	hs
100s	10s	1s	100	10s	1s	100	10s	1s		
			s			s				
								0	0	1
								0	1	
								1		
							1	0		
						1	0	0		
					1	0	0	0		
				1	0	0	0	0		
			1	0	0	0	0	0		
		1	0	0	0	0	0	0		
	1	0	0	0	0	0	0	0		

1,000,000	2,000,000	3,000,000	4,000,000	5,000,000	6,000,000	7,000,000	8,000,000	9,000,000
100,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
10,000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

									0		0	1	one hundredth
									0	2	1		one tenth
									1				one
								1	0				ten
							1	0	0				one hundred
					1	,	0	0	0				one thousand
				1	0		0	0	0				ten thousand
			1	0	0	e	0	0	0				one hundred thousand
	1	,	0	0	0	e	0	0	0				one million
1	0	,	0	0	0	,	0	0	0				ten million

Recognise that the 1 becomes ten times the size as it moves from right to left in a place value chart.

Recognise that 1 becomes one-tenth the size as it moves from left to right in a place value chart.

Recognise that the 1 becomes 10 times the size as it moves up in a Gattegno chart.

Recognise that 1 becomes one-tenth the size as it moves down in a Gattegno chart.



Recognise that:

10 hundredths are equivalent to 1 tenth.

10 tenths are equivalent to 1 one.

10 ones are equivalent to 1 ten.

10 tens are equivalent to 1 hundred.

10 hundreds are equivalent to 1 thousand.

10 thousands are equivalent to 1 ten thousand.

10 ten thousands are equivalent to 1 hundred thousand.

10 hundred thousands are equivalent to 1 million.

10 millions are equivalent to 1 ten million.





Number and Place Value	Vocabulary:
Year 6	Ones Tens Hundreds Thousands Ten-thousands Hundred-thousands Millions Ten-Millions Tenths Hundredths Represents Digit Place Value
Powers of 10 (2)	Counters Gattegno Tens Frame Equivalent Equation Multiply Divide
	Ten/hundred times the size One-tenth/hundredth times the size

	10,000,000	20,000,000	30,000,000	40,000,000	50,000,000	60,000,000	70,000,000	80,000,000	90,000,000
	1,000,000	2,000,000	3,000,000	4,000,000	5,000,000	6,000,000	7,000,000	8,000,000	9,000,000
	100,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
	10,000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
	1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
C	100	200	300	400	500	600	700	800	900
+	10	20	30	40	50	60	70	80	90
	1	2	3	4	5	6	7	8	9
-	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

Explore the Gattegno chart and recognise numbers that are one hundred times the size and one-hundredth times the size.

Ten is one hundred times the size of 0.1. 0.1 multiplied by 100 is equal to 10. 0.1 is one-hundredth of the size of 10. 10 divided by 100 is equal to 0.1.

	1,000s	100s	10s	1s	0.1s	0.01s	0.001s
100			2	5			
÷ 100 t			0	0	2	5	

0.25	×	100	=	25
25	÷	100	=	0.25

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.001	0.002	0.003	0.004	0.005	0.006	0.007	0.008	0.009

Use the Place Value chart and Gattegno chart to support children to visualise multiplying and dividing by 10, 100 or 1000.

25 is one hundred times the size of 0.25. 0.25 multiplied by 100 is equal to 25. 0.25 is one-hundredth of the size of 25. 25 divided by 100 is equal to 0.25.

Scaling Models

Number and Place Value

Year 6

Place Value in Numbers up to 10,000,000.

Vocabulary:

Thousands Ten-thousands Hundred-thousands Ones Tens Hundreds Millions Ten-Millions Hundredths Digit Place Value Tenths Represents Counters Gattegno Partition Combine Equation Addend Sum Minuend Subtrahend Difference



Form numbers to 10,000,000 using place value counters and the part-part-whole model. The 2 represents 2 tens The 9 represents 9 hundreds The 3 represents 3 hundred thousands.

Write as an additive equation.



	10 10 1 01 01	
30,051.2		30 thousand and 51 and 2 tenths

1,000	,000	2,000,000	3,000,000	4,000,000	5,000,000	6,000,000	7,000,000	8,000,000	9,000,000
100,	,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
10,	000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
1,	000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
83	100	200	300	400	500	600	700	800	900
	10	20	30	40	50	60	70	80	90
3	1	2	3	4	5	6	7	8	9
62	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.0

Make connections between different representations of numbers to 10,000,000 with the Gattegno Chart.

Millions			Th	ousan	ıds	Ones			
100s	00s 10s 1s		100s	10s	1s	100s	10s	1s	
					1	9	3	7	
				5	1	9	3	7	
			4	5	1	9	3	7	
		5	4	5	1	9	3	7	

Read numbers to 10,000,000. Focus on the structure of millions, thousands and ones.

5 million, four hundred and fifty one thousand, nine hundred and thirty one (ones).

3,870,291.46

Millions		Thousands			Ones					
100s	10s	1s	100s	10s	1s	100s	10s	1s	0.1s	0.01s
		3	8	7	0	2	9	1	4	6

Recognise the value of each digit. The 3 represent 3 million.



Number and Place Value	Vocabulary:
Year 6	Ones Tens Hundreds Thousands Ten-thousands Hundred-thousands Millions Ten-Millions Tenths Hundredths Represents Digit Place Value Intervals Scales Divisions
Reading Scales with 2, 4, 5, or 10 intervals	Equal Parts Whole Value Bar model Plus Minus Multiply Divide Grams Millilitres Litres Grams Kilograms Metres Centimetres Estimate



Addition and Subtraction Vocabulary: Year 6 Additive Multiplicative Relationship Represents Compose Combine Total More than Less than Plus + Minus - Equal to = Addition Subtraction Divide ÷ Multiply x One-____of Equation Expression Bar Model Whole Part Difference Multiplier Unknown Sequence Addend + Addend = Sum









Addition and Subtraction	Vocabulary:		
Year 6	Additive Multiplicative Relationship Represents Compose Combine Total More than Less than Plus + Minus - Equal to = Addition Subtraction Divide ÷		
Quantify additive and multiplicative relationships	Multiply x Oneof Equation Expression Bar Model Whole Part Difference Multiplier Unknown Sequence		
	Addend + Addend = Sum		

 $\frac{1}{3}$ of ?= 10



30		
10	10	10

whole by recognising		
how many parts the		
hole has been divided		
into.		

$$\frac{1}{3}$$
 of 30 = 10







b

b

one part = 20 ÷ 5 = 4

b = 4

a = 4 × 4 = 16

The two numbers are 9 and 16.

a = 9 + 7 = 16

The two numbers are 16 and 4.



÷ 100

÷ 100

- 0.4

0.4 _

Addition, Subtraction, Multiplication and Division	Vocabulary:
Year 6	Additive Multiplicative Relationship Represents Compose Combine Total
Quantify additive and multiplicative relationships	More thanLess thanPlus +Minus -Equal to =AdditionSubtractionDivide÷ Multiply xOneofEquationExpressionBar ModelWholePart DifferenceMultiplierUnknownSequence
$ \frac{1}{3}$ of ?= 10	Addend + Addend = SumFactor x Factor = Product (Multiplicand x Multiplier = Product)Minuend – Subtrahend = DifferenceDividend ÷ Divisor = Quotient



 $\frac{1}{3}$ of 30 = 10



Addition and Subtraction

Year 6

Solve Problems involving Ratio Relationship

Vocabulary:

AdditiveMultiplicativeRelationshipRepresentsEquationUnknownScale-factorRatioRatioTable_______times the sizeone-_____the size ofVertical Horizontal

Factor x Factor = Product (Multiplicand x Multiplier = Product)

Dividend ÷ Divisor = Quotient





The two numbers are 9 and 16.

The two numbers are 16 and 4.

Fractions

Year 6

Simplify Fractions

Vocabulary:

FractionNotationDividedEqualNumeratorDenominatorWholePartsFraction Bar (Vinculum)HalfThirdQuarterFifthSixthSeventhEighthNinthTenthOne-____MultipleFactorCommonSimplifySimplest FormMixed NumberImproper FractionHighest Common Factor





Recap equivalent fractions with multiple representations. Identify a fraction in its simplest form when the only common multiple of both the numerator and denominator is 1.

 $\frac{1}{4}$ is in its simplest form. I know this because the only common factor of the numerator and the denominator is 1.



8

÷2

÷2

<u>4</u> 12

÷4

 $\div 4$

3

12

9

12

12

16

÷1

÷1

12

 $\frac{4}{12}$

 $\frac{2}{6}$

Extend to fractions where the numerator in the simplest form is greater than 1. $\frac{3}{4}$ is in its simplest form. I know this because the only common factor of the numerator and the

denominator is 1.

Finding the common factors of both the numerator and denominator allows us to simplify each fraction to its simplest form.

The common factors of 4 and 12 are 1, 2 and 4.

The highest common factor is 4.

Generalisation:

Dividing both the numerator and the denominator of a fraction by their highest common factor converts the fraction to its simplest form.





Improper fraction can be simplified before or after they are converted to a mixed number. The highest common factor of 20 and 12 is 4. The highest common factor of 8 and 12 is 4.



÷4

=

÷4

<u>5</u> 3

<u>20</u> 12



Fractions

Year 6

Compare Fractions with Different Denominators

Vocabulary: Fraction Notation Divided Equal Numerator Denominator Whole Parts Fraction Bar (Vinculum) Half Third Quarter Fifth Sixth Seventh Multiple Common Denominator Ninth Tenth One-___ Convert Express

Proportion Estimate Position Number Line Greater than Less than



9

 $\frac{1}{3}$ 3

is about here. I imagined the

ne divided into 3 equal parts.



Generalisations:

If the numerators are both 1, then the larger the denominator,

the smaller the fraction.

The denominator represents the number of equal parts the

whole has been split into. The greater this number, the more

equal parts and therefore the smaller the size of each part.

is about here. I imagined the line divided into 4 equal parts and then pictured 3 of them. 3 is quite

a big part of 4, so $\frac{3}{4}$ is nearer to 1.



We can compare fractions and mixed numbers with the same numerator in different ways



We can use our knowledge of fractions on a number line to help estimate and compare their relative size.



Eighth



We can reason about the proportional size of the numerator in relation to the denominator to compare fractions. 5 is a larger part of 6 than 7 is of 11, which means $\frac{5}{6}$ is greater than $\frac{7}{11}$

11

5 6



0